

Modern Algebra I: Group Theory

Examples of Groups

Set	Operation	Order	Description	Identity	Inverse	Abelian?	Cyclic?	Other Notes (isomorphic groups, etc.)
D_3								Isomorphic to the set of functions generated by $f(x) = \frac{1}{x}, g(x) = \frac{1}{1-x}$ under composition
D_4								
V_4								
S_3			Permutations of a three element set $\{a, b, c\}$, for example)					Isomorphic to D_3
\mathbb{Z}								
$\{1, -1\}$								

Modern Algebra I: Group Theory

Examples of Groups

Set	Operation	Order	Description	Identity	Inverse	Abelian?	Cyclic?	Other Notes (isomorphic groups, etc.)
$\{1, -1, i, -i\}$								
\mathbb{R}^\times								
\mathbb{Z}_n		Number of $\{1, \dots, n-1\}$ relatively prime to n						
\mathbb{Z}_n^\times							In some cases, but not in general	
$M_2(\mathbb{R})$								
$GL(2, \mathbb{R})$								

Modern Algebra I: Group Theory

Examples of Groups

Set	Operation	Order	Description	Identity	Inverse	Abelian?	Cyclic?	Other Notes (isomorphic groups, etc.)
$SL(2, \mathbb{R})$								
$GL(2, \mathbb{Z}_2)$								